Name Class



www.MathsTeacherHub.com

Algebraic proof

(9 - 1) Topic booklet

HIGHER

These questions have been collated from previous years GCSE Mathematics papers.

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Total Marks

Instructions

- •Use black ink or ball-point pen.
- •Fill in the boxes at the top of this page with your name, centre number and candidate number.
- •Answer all questions.
- •Answer the questions in the spaces provided
- there may be more space than you need.
- •Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.
- •If the question is a **1F** question you are not allowed to use a calculator.
- •If the question is a **2F** or a **3F** question, you may use a calculator to help you answer.

Information

- •The marks for **each** question are shown in brackets
- use this as a guide as to how much time to spend on each question.

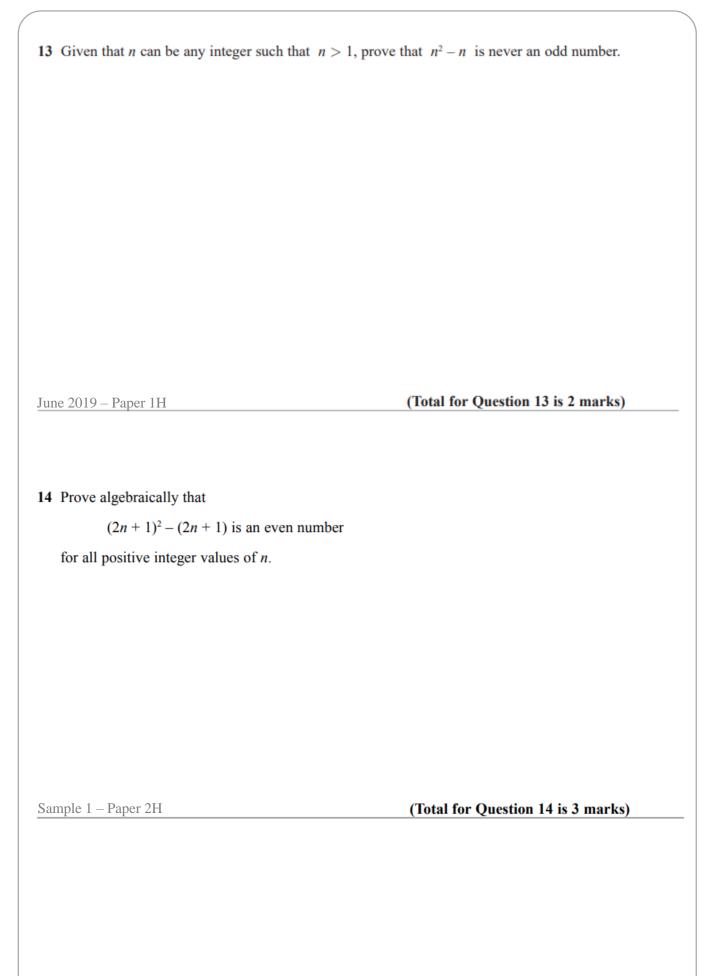
Advice

- •Read each question carefully before you start to answer it.
- •Keep an eye on the time.
- •Try to answer every question.
- •Check your answers if you have time at the end.

Answer ALL questions Write your answers in the space provided. You must write down all the stages in your working.

12 Prove that the square of an odd number is always 1 more than a multiple of 4
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)
June 2018 – Paper 1H (Total for Question 12 is 4 marks)

2



15 Prove algebraically that the sum of the squares of any always a multiple of 4	two consecutive even numbers is
November 2019 – Paper 3H	(Total for Question 15 is 3 marks)

15 Prove algebraically that the difference between the squ numbers is always a multiple of 8	uares of any two consecutive odd
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)
November 2018 – Paper 3H	(Total for Question 15 is 3 marks)

vember 2022 – Paper 1F	Ι	(Total for Question 16 is 4 ma	rks)
			(1)
You must give reas	ons for your answer.		
odd numbers must be a (b) Is Sophia correct?	і шипіріе 01 4		
		e difference of the squares of any two	
			(3)
	$(2m+1)^2 - (2n-1)^2 =$		

					.4
16	n 1S	an	integer	greater	than

Prove algebraically that $n^2 - 2 - (n-2)^2$ is always an even number.

May 2017 – Paper 1H

(Total for Question 16 is 4 marks)

17 n is an integer.

Prove algebraically that the sum of $\frac{1}{2}n(n+1)$ and $\frac{1}{2}(n+1)(n+2)$ is always a square number.

November 2017 – Paper 1H

(Total for Question 17 is 2 marks)

17 The product of two consecutive positive integers is add integers.	ded to the larger of the two
Prove that the result is always a square number.	
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)
Specimen 2 – Paper 3H	(Total for Question 17 is 3 marks)

20 Prove algebraically that the difference between the squintegers is equal to the sum of these two integers.	nares of any two consecutive	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	
Specimen 1– Paper 1H	(Total for Question 20 is 4 marks)	

Prove that the difference		13 e sanares			of the sequence is always
a multiple of 24	between th	c squares	of any to	vo terms	of the sequence is always
ecimen 1 – Paper 3H				(Total	for Question 22 is 6 marks)

22 Here are the first five terms of an arithmetic sequence.